### Survival Analysis Part I

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- First, I will review data complications.
- Second, I will review study design complications.
- Third, I will review basic survival analyses.
- Fourth, I will conclude with an example in Stata.

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- Survival analysis requires very specific data formatting.
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• Such formatting is a key part of "cleaning" the data for analysis.

#### Data Notation

Typically, we need to create:

$$Y_i$$
 = the duration until the event occurs, ie. 12 months

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- Date variables need to be converted to date format using the date() command.

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- 3. Date might be recorded as 31jan2000 or 1/31/2000.
- 4. You must know the difference.

• The date command: date(string, "FMT", 201X)

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- Key parts FMT and 201X

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- The date command: date(string, "FMT", 201X)
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- gen date1 = date(date-string-var, "DMY", 2019)

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- FMT is DMY for 31jan2000.
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- Final part is topyear-most recent year in your data.

• Stata saves dates as number of days since Jan 1, 1960.

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- The command:
- format date1 %td
- converts date from numeric form to date format.

### Calculating Duration

- Stata: gen duration = date2 date1
- This gives survival time in days.

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• Most common is administrative censoring.

#### Administrative Censoring

• Survival analysis requires a stopping point data collection.

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- Survival analysis requires a stopping point data collection.
- Some patients may not have experienced the event when the data is collected.
- For these patients, we don't observe their survival time.
- We have a duration but survival time is missing, since the recorded time span is qualitatively different from patients that experienced the event.

• Outcome: disease free survival after adj. chemo.

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• The survival time is missing.

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• We must record observations that are censored.

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- Create new variable: C = 1 is an uncensored observation, C = 0 is a censored observation.

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- Need to be defined by the researcher.
- Widespread competing events makes interpretation of results difficult.

### Effects of Censoring

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- If censoring is systematic, estimates from multivariate models can be biased.

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#### **Baseline Time Point**

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- All subjects should be untreated at t = 0.
- E.g.: Effect of lipitor on time to cardiac event.
- No one should be on lipitor at t = 0.

### Example Data

id	duration	censor
1	4	1
2	2	1
3	5	1
4	6	0

#### Stata stset

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- Syntax: stset surv\_var, failure(censor)

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- Stata requires all survival data to be stset.
- Syntax: stset surv\_var, failure(censor)
- $\bullet$  Stata creates: \_t0, \_t1, \_d, and \_st
- time span, censoring, and relevant.

• Survival curves are basic summary statistics.

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- Survival curves are basic summary statistics.
- Kaplan-Meier method is the most common.

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- Survival curves are basic summary statistics.
- Kaplan-Meier method is the most common.
- Displays probability of event for those at risk.

- We have *N* observations.
- $n_t$  = the number of observations "at risk" for the event at time t.

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- We have *N* observations.
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- *d<sub>t</sub>* = the number of observations which experience the event at time *t*
- For any particular time t = k, we can get an estimate of the survival function S(t) as the product of the conditional proportions of all survivors to that point

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This is known as the "Kaplan-Meier" estimate of the survivor function.

# Estimating Survival Curves - An Example

Time	No. at risk	No. failed	No. censored
2	6	1	0
4	5	2	0
5	3	0	1
7	2	1	0
8	1	0	1

### Estimating Survival Curves

Time	No. at risk	No. failed	No. censored	р	$\hat{S}(t)$
2	6	1	0	5/6	5/6
4	5	2	0	3/5	1/2
5	3	0	1	1	1/2
7	2	1	0	1/2	1/4
8	1	0	1	1	1/4

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	7	2	1	0	1/2	1/4
	8	1	0	1	1	1/4
(6-1) 5						

$$\frac{(5-1)}{6} = \frac{5}{6}$$
$$\frac{(5-2)}{5} = \frac{3}{5} \times \frac{5}{6} = \frac{1}{2}$$

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• Typically, we plot stratified KM curves.

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- Stratify by key covariate: treatment, sex, etc.
- Inference is now important: are the curves statistically different?

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If we're interested in inference, or just want to know the uncertainty surrounding our estimates, we need some measure of the variability of these estimates. The most commonly-used of these is the "Greenwood" variance estimator:

$$Var[\widehat{S(t_k)}] = [\widehat{S(t_k)}]^2 \sum_{t \le t_k} \frac{d_t}{n_t(n_t - d_t)}$$

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We have two groups; *treatment* (=1) and *placebo* (=0), and we want to know if the survival curves are statistically different. Standard test is the log-rank test.

	Treatment	Placebo	Total
Event	$d_{1t}$	d <sub>0t</sub>	dt
No Event	$n_{1t} - d_{1t}$	$n_{0t} - d_{0t}$	$n_t - d_t$
Total	$n_{1t}$	n <sub>0t</sub>	n <sub>t</sub>

Normally, we'd do a  $\chi^2$  test here, using the observed and expected number of events per cell.

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The same general intuition applies, except that we conduct a similar test for each time period t.

$$\hat{e}_{1t} = \frac{n_{1t}d_t}{n_t}$$

is the "expected" number of events in that time period.

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$$\hat{Q} = \frac{\left[\sum_{t} (d_{1t} - \hat{e}_{1t})\right]^2}{\left[\frac{n_{1t}n_{0t}d_{0t}(n_t - d_t)}{n_t^2(n_t - 1)}\right]}$$

The numerator of  $\hat{Q}$  is the sum of the (squared) observed minus expected events. We use this to test the null hypothesis of no difference between the treatment and placebo groups.

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 $\hat{Q}$  is distributed as  $\chi_1^2$ .

## Unadjusted Survival Analysis

- The analysis thus far assumes treated and control groups are exchangeable.
- Only reason survival curves differ is treatment-not some baseline characteristic of the treated group.
- Next time we take up methods to control for confounders.

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### Conclusion

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- Data cleaning is a key step in survival analysis.
- May require several consequential choices.